

# Parametry nosníku

```
In[153]:= Remove["Global`*"];
```

```
In[154]:= younguvModul = 210 * 109; sirka = 0.02; vyska = 0.00094; delka = 0.203;
```

```
momentSetrvacnostiPrurezu =  $\frac{1}{12}$  sirka * vyska3; hustotaOceli = 7800; plocha = sirka * vyska;
```

## Mód 1

### Konstanta k (řešení transcendentní rovnice)

```
In[155]:= n = 1; k[n] =  $\frac{1.875}{delka}$ ;
```

### Úhlová frekvence $\Omega$ , frekvence f

```
In[156]:=  $\Omega[n] = k[n]^2 * \sqrt{\frac{younguvModul * momentSetrvacnostiPrurezu}{hustotaOceli * plocha}}$ 
```

```
Out[156]:= 120.119
```

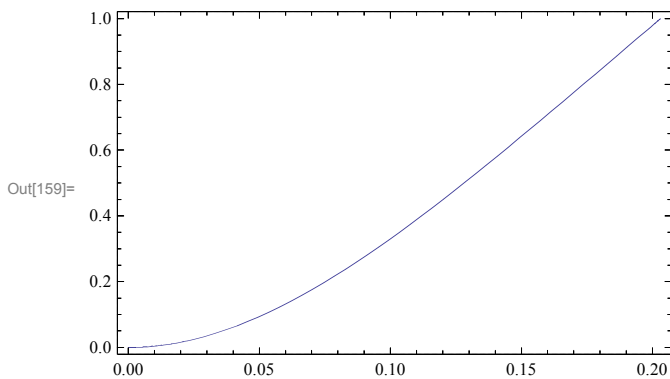
```
In[157]:=  $f[n] = \frac{\Omega[n]}{2 * \pi}$ 
```

```
Out[157]:= 19.1175
```

### Průhybová křivka (normalizovaná)

```
In[158]:= w[n][x_] = (Sinh[k[n] * delka] + Sin[k[n] * delka]) * (Cosh[k[n] * x] - Cos[k[n] * x]) -  
(Cosh[k[n] * delka] + Cos[k[n] * delka]) * (Sinh[k[n] * x] - Sin[k[n] * x]);
```

```
In[159]:= Plot[ $\frac{w[n][x]}{w[n][delka]}$ , {x, 0, delka}, Frame -> True]
```



## Mód 2

### Konstanta k (řešení transcendentní rovnice)

```
In[160]:= n = 2; k[n] =  $\frac{4.694}{\text{delka}}$ ;
```

### Úhlová frekvence $\Omega$ , frekvence f

```
In[161]:=  $\Omega[n] = k[n]^2 * \sqrt{\frac{\text{younguvModul} * \text{momentSetrvacnostiPrurezu}}{\text{hustotaOceli} * \text{plocha}}}$ 
```

```
Out[161]= 752.824
```

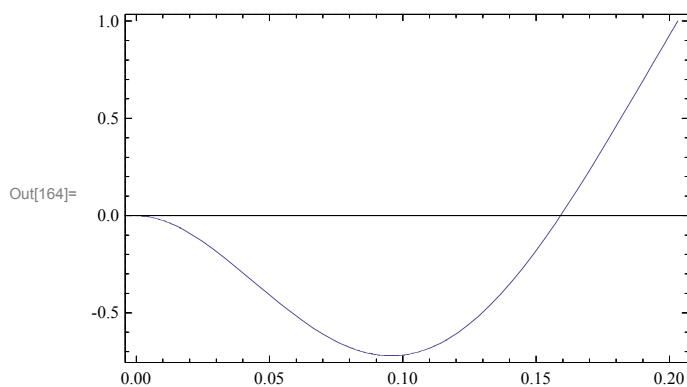
```
In[162]:=  $f[n] = \frac{\Omega[n]}{2 * \pi}$ 
```

```
Out[162]= 119.816
```

### Průhybová křivka (normalizovaná)

```
In[163]:=  $w[n][x_] = (\text{Sinh}[k[n] * \text{delka}] + \text{Sin}[k[n] * \text{delka}]) * (\text{Cosh}[k[n] * x] - \text{Cos}[k[n] * x]) -$   
 $(\text{Cosh}[k[n] * \text{delka}] + \text{Cos}[k[n] * \text{delka}]) * (\text{Sinh}[k[n] * x] - \text{Sin}[k[n] * x]);$ 
```

```
In[164]:=  $\text{Plot}[\frac{w[n][x]}{w[n][\text{delka}]}, \{x, 0, \text{delka}\}, \text{Frame} \rightarrow \text{True}]$ 
```



### Umístění uzlu

```
In[165]:=  $\text{FindRoot}[w[n][x] == 0, \{x, 0.1\}]$ 
```

```
Out[165]= {x -> 0.159042}
```

## Mód 3

### Konstanta k (řešení transcendentní rovnice)

```
In[166]:= n = 3; k[n] =  $\frac{(2 * n - 1) * \pi}{2 * \text{delka}}$ ;
```

### Úhlová frekvence $\Omega$ , frekvence f

```
In[167]:=  $\Omega[n] = k[n]^2 * \sqrt{\frac{\text{younguvModul} * \text{momentSetrvacnostiPrurezu}}{\text{hustotaOceli} * \text{plocha}}}$ 
```

```
Out[167]= 2107.6
```

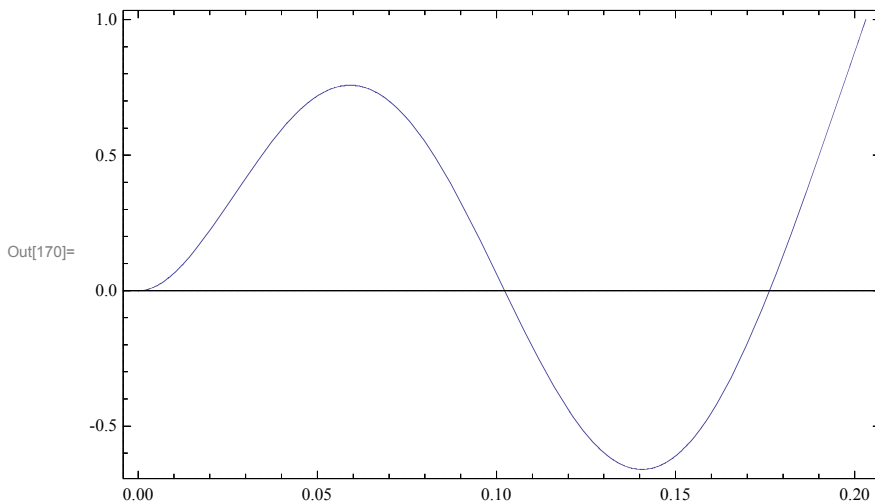
```
In[168]:=  $f[n] = \frac{\Omega[n]}{2 * \pi}$ 
```

```
Out[168]= 335.434
```

### Průhybová křivka (normalizovaná)

```
In[169]:=  $w[n][x_] = (\text{Sinh}[k[n] * \text{delka}] + \text{Sin}[k[n] * \text{delka}]) * (\text{Cosh}[k[n] * x] - \text{Cos}[k[n] * x]) -$   
 $(\text{Cosh}[k[n] * \text{delka}] + \text{Cos}[k[n] * \text{delka}]) * (\text{Sinh}[k[n] * x] - \text{Sin}[k[n] * x]);$ 
```

```
In[170]:=  $\text{Plot}[\frac{w[n][x]}{w[n][\text{delka}]}, \{x, 0, \text{delka}\}, \text{Frame} \rightarrow \text{True}]$ 
```



### Umístění uzlů

```
In[171]:=  $\text{FindRoot}[w[n][x] == 0, \{x, 0.1\}]$ 
```

```
Out[171]= {x → 0.10223}
```

```
In[172]:=  $\text{FindRoot}[w[n][x] == 0, \{x, 0.18\}]$ 
```

```
Out[172]= {x → 0.176156}
```

## Mód 4

### Konstanta k (řešení transcendentní rovnice)

```
In[173]:= n = 4; k[n] =  $\frac{(2 * n - 1) * \pi}{2 * \text{delka}}$ ;
```

### Úhlová frekvence $\Omega$ , frekvence f

```
In[174]:=  $\Omega[n] = k[n]^2 * \sqrt{\frac{\text{younguModul} * \text{momentSetrvacnostiPrurezu}}{\text{hustotaOceli} * \text{plocha}}}$ 
```

```
Out[174]= 4130.89
```

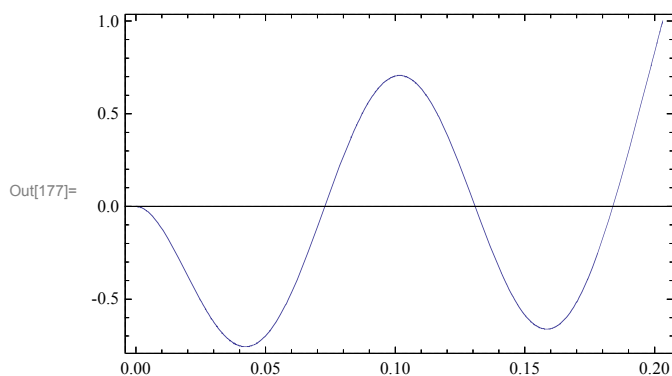
```
In[175]:=  $f[n] = \frac{\Omega[n]}{2 * \pi}$ 
```

```
Out[175]= 657.451
```

### Průhybová křivka (normalizovaná)

```
In[176]:=  $w[n][x_] = (\text{Sinh}[k[n] * \text{delka}] + \text{Sin}[k[n] * \text{delka}]) * (\text{Cosh}[k[n] * x] - \text{Cos}[k[n] * x]) -$   
 $(\text{Cosh}[k[n] * \text{delka}] + \text{Cos}[k[n] * \text{delka}]) * (\text{Sinh}[k[n] * x] - \text{Sin}[k[n] * x]);$ 
```

```
In[177]:=  $\text{Plot}[\frac{w[n][x]}{w[n][\text{delka}]}, \{x, 0, \text{delka}\}, \text{Frame} \rightarrow \text{True}]$ 
```



### Umístění uzlů

```
In[178]:=  $\text{FindRoot}[w[n][x] == 0, \{x, 0.06\}]$ 
```

```
Out[178]= {x → 0.0727423}
```

```
In[179]:=  $\text{FindRoot}[w[n][x] == 0, \{x, 0.14\}]$ 
```

```
Out[179]= {x → 0.130749}
```

```
In[180]:=  $\text{FindRoot}[w[n][x] == 0, \{x, 0.18\}]$ 
```

```
Out[180]= {x → 0.183829}
```